

# *Optimal Use of Information for Measuring Top Quark Properties*



**Florencia Canelli**

**University of Rochester**



- Applied to  $M_{\text{top}}$  and  $F_0$  measurement using Run I DØ data

$$M_{\text{top}} \text{ (preliminary)} = 180.1 \pm 5.4 \text{ GeV}$$

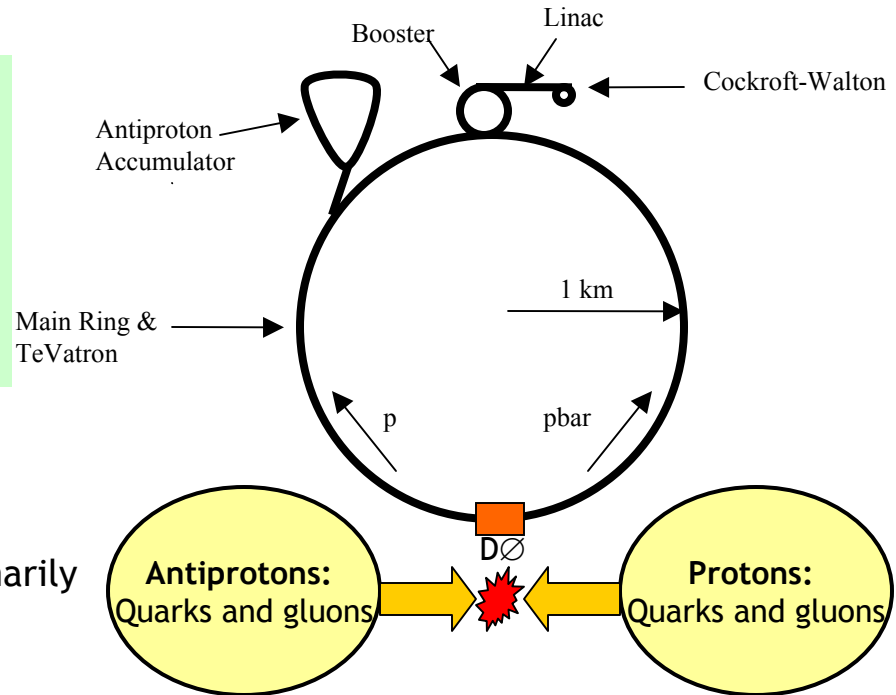
$$F_0 \text{ (preliminary)} = 0.56 \pm 0.31$$

# Top Quark Production

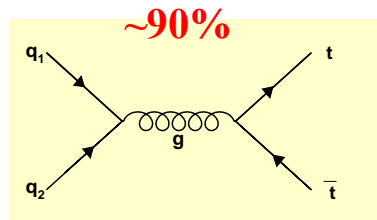
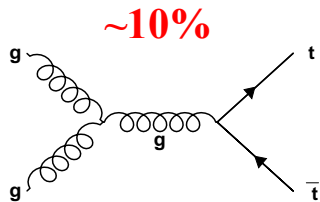
- Discovered in 1995 by DØ and CDF collaborations at the **Fermilab TeVatron**

## Fermilab TeVatron 1992-1996 (Run I)

- $\sqrt{s} = 1.8\text{TeV}$ , 900 GeV protons  
- 900 GeV antiprotons
- 6 x 6 protons-antiprotons bunches



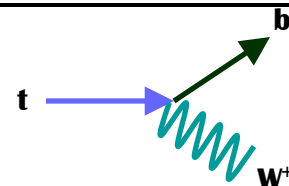
- In proton-antiproton collisions at TeVatron energies, top quarks are primarily **produced in pairs**.  
@  $\sqrt{s} = 1.8\text{TeV}$ :



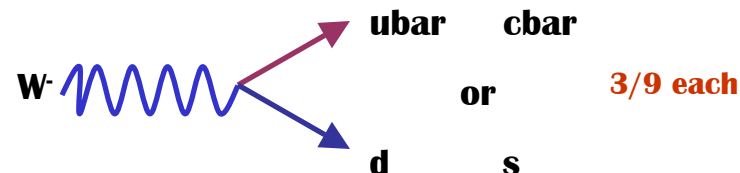
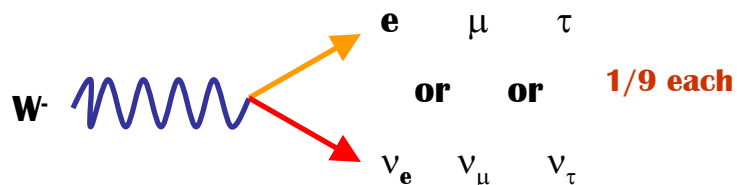
Each parton carries a fraction of the total energy (900 GeV)

# Top Quark Decay

- Each top quark decays weakly:  $BR(t \rightarrow Wb) @ 100\%$



- W's can decay in any of these ways:



- From a ttbar pair, we have a W<sup>+</sup> and a W<sup>-</sup>. There are 3 main experimental ttbar signatures depending on the decay of the W boson:

**Dilepton**  $BR(ee + \mu\mu + e\mu) = 5\%$

small background, small statistics  
2 leptons, 2 b quarks, 2 neutrinos

**Lepton + Jets**  $BR(e+jets, \mu+quarks) = 30\%$   
manageable backgrounds, higher statistics  
1 lepton, 4 quarks, 1 neutrino

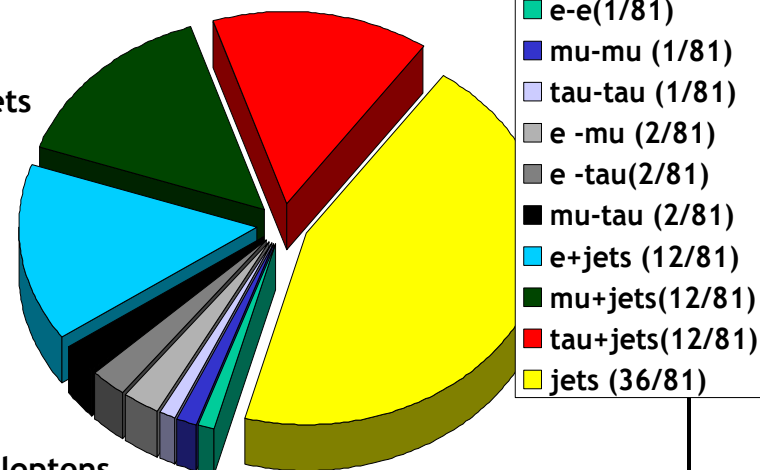
**All-Hadronic**  $BR(quarks) = 44\%$

multi-jets background  
6 quarks (2 b quarks)

lepton+jets

dileptons

all-hadronic



# Detecting Top Quarks

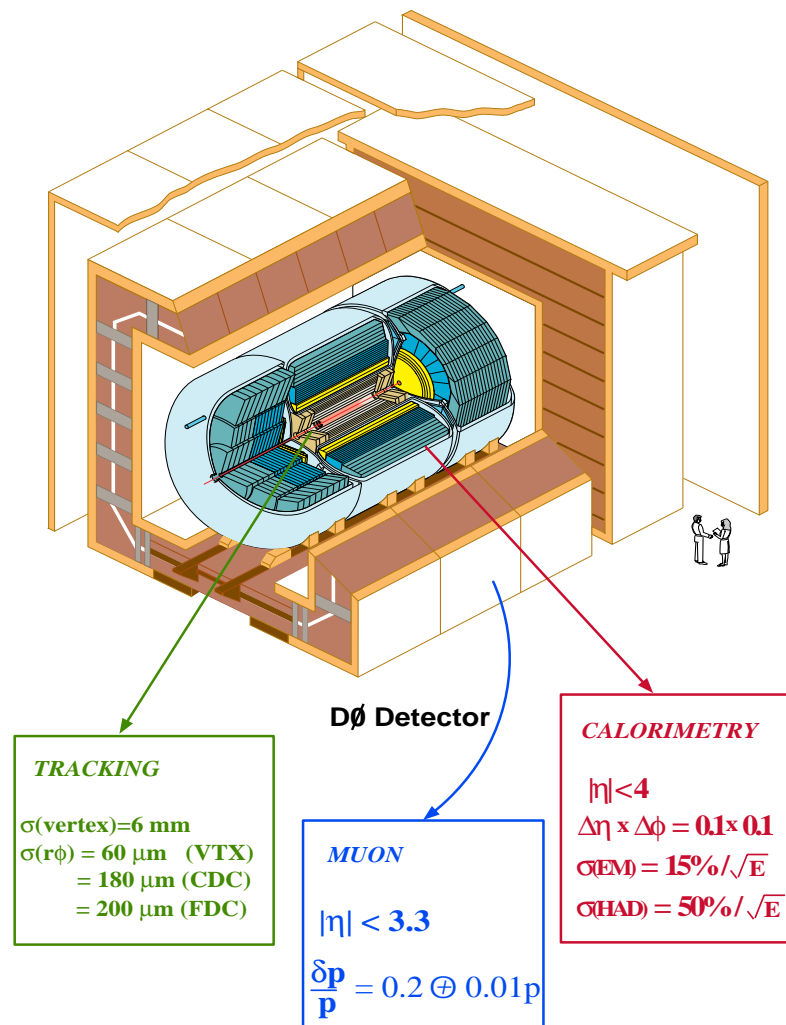
- **Detector located around the collision point:**

1. Measure particle's position, momentum and charge
2. Type and kinetic energy

- **DØ Run I Detector**

Starting from center moving outwards:

- o **Central tracking system:** measures interaction vertex
- o **Calorimeters:** contain and measure energy and direction of electromagnetic/hadronic particles (electron, photon, jets)
- o **Muon Chambers (toroid):** charge/momentum of muons



$\eta$  is proportional to the polar angle,  $\theta$   
 $P_T$  = transverse momentum

# Event Topology and Selection Criteria

- DØ Statistics Run I (125 pb<sup>-1</sup>)

**Signature:** 1 high- $P_T$  lepton, 4 jets (2 b jets), large missing- $E_T$

*More jets coming from gluon radiation, or fewer due to detector inefficiencies, merging of jets, etc*

**Background:** W with associated production of jets

- **Standard Selection:**

- **Lepton:**  $E_T > 20 \text{ GeV}$ ,  $|\eta^e| < 2$ ,  $|\eta^\mu| < 1.7$
- **Jets:**  $\geq 4$ ,  $E_T > 15 \text{ GeV}$ ,  $|\eta| < 2$
- **Missing  $E_T > 20 \text{ GeV}$**
- " $E_T^W$ "  $> 60 \text{ GeV}$ ;  $|\eta_W| < 2$

**91 events**

Ref. PRD 58 (1998), 052001

**Background:** W+jets (~85%) + multijet (~15%)

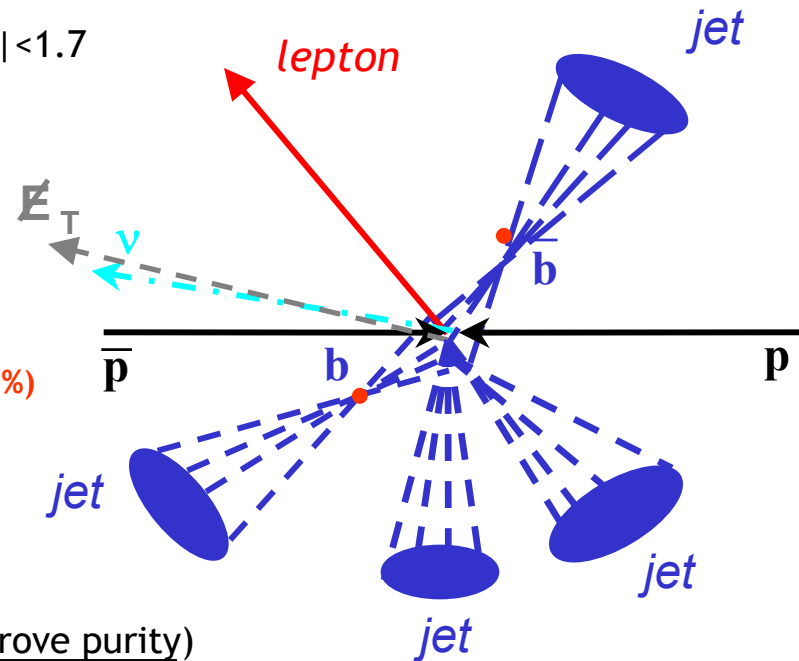
- **Additional cuts for this analysis :**

- 4 Jets only (LO ME)

**71 events**

- Background probability (to improve purity)

**22 events => 12 signal + 10 background**



# The General Method - the ideal case

- We want to find the value of a parameter  $\alpha$
- The best estimate of a **parameter ( $\alpha$ )** is achieved comparing the events with the probability from the theory with the data. This is done by maximizing a likelihood:

In our case  $\alpha = M_{\text{top}}, F_0$

$$L(\alpha) = e^{-N \int \bar{p}(x; \alpha) dx} \prod_{i=1}^N \bar{P}(x_i; \alpha)$$

where  $x$  is a set of measured variables

- If we could **access all parton level quantities** in the event (the four momentum for all final and initial state particles), then

$$\bar{P}(x; \alpha) \propto d\sigma$$

That is, we could simply **evaluate the differential cross section as a function of the parameter that we would like to extract for these partons**. In this way we would be using the best knowledge of the physics involved

# The General Method - the real case

- In a real experiment, we take the ideal case and **integrate over everything we do not know**. The integration reflects the fact that **we want to sum over all the possible parton variables  $y$  leading to the observed set of variables  $x$**

$d^n\sigma$  is the differential cross section

$W(y,x)$  is the probability that a parton level set of variables  $y$  will be measured as a set of variables  $x$

$$\bar{P}(x;\alpha) = \frac{1}{\sigma} \int d^n\sigma(y;\alpha) \frac{dq_1 dq_2 f(q_1) f(q_2)}{f(q_1) f(q_2)} W(x,y)$$

$f(q)$  is the probability distribution that a parton will have a momentum  $q$

- In a real experiment with a **real detector**

$$\bar{P}_{measured}(x;\alpha) = Acc(x) \bar{P}_{production}(x;\alpha)$$

where  $Acc(x)$  include all conditions for accepting or rejecting an event

- If we have **background** events with weights  $c_i$

$$\bar{P}(x; c_1, \dots, c_K, \alpha) = \sum_{i=1}^K c_i \bar{P}_i(x; \alpha)$$

# Transfer Function $W(x,y)$

- $W(x,y)$  probability of measuring  $x$  when  $y$  was produced ( $x$  jet variables,  $y$  parton variables):

Energy of **electrons** is considered well measured

$$W(x,y) = \delta^3(p_e^y - p_e^x) \prod_{j=1}^4 W_{jet}(E_j^y, E_j^x) \prod_{i=1}^4 \delta^2(\Omega_i^y - \Omega_i^x)$$

And due to the excellent granularity of the DØ calorimeter, **angles** are also considered well measured

where

$E^y$	energies of produced quarks
$E^x$	measured and corrected jet energies
$p_e^y$	produced electron momenta
$p_e^x$	measured electron momenta
$\Omega_j^y, \Omega_j^x$	produced and measured jet angles

- Events with muons are integrated over their resolution



# $t\bar{t} \rightarrow l + \text{jets}$ Matrix Element

$$|M|^2 = \frac{g_s^4}{9} F \bar{F} (2 - \beta^2 s_{qt}^2)$$

Only  $q\bar{q}$  ~90%

no  $t\bar{t}$  spin correlation included

$s_{qt}$  sine of angle between incoming parton (q) and top quark in the  $q\bar{q}$  CM

$\beta$  top quark's velocity in the  $q\bar{q}$  CM

$g_s$  strong coupling constant

**Leptonic decay**  $F = \frac{g_w^4}{4} \left[ \frac{m_t^2 - m_{ev}^2}{(m_t^2 - M_t^2)^2 + (M_t \Gamma_t)^2} \right] \left[ \frac{\omega(\cos \varphi_{eb}^-)}{(m_{ev}^2 - M_W^2)^2 + (M_W \Gamma_W)^2} \right]$

**Hadronic decay**  $\bar{F} = \frac{g_w^4}{4} \left[ \frac{m_t^2 - m_{d\bar{u}}^2}{(m_t^2 - M_t^2)^2 + (M_t \Gamma_t)^2} \right] \left[ \frac{\omega(\cos \varphi_{d\bar{b}})}{(m_{d\bar{u}}^2 - M_W^2)^2 + (M_W \Gamma_W)^2} \right]$

$M_t, M_W$  pole top and W mass

$m_t$  top mass in any event

$m_{en}, m_{du}$  invariant mass of the  $en$  and  $du$  (or  $cs$ ) system

$G_t, G_W$  top and W width

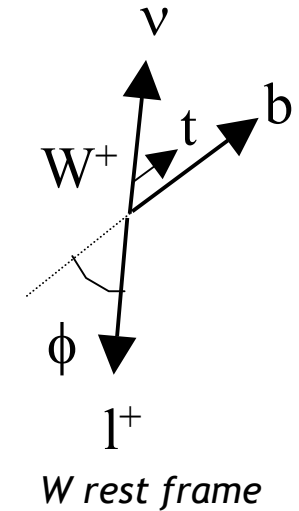
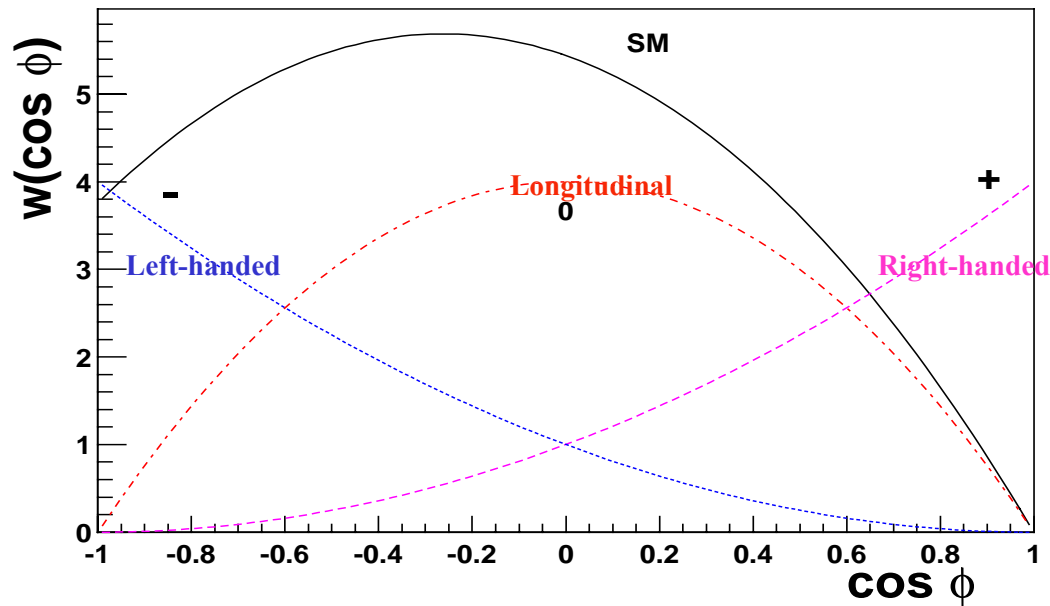
$g_W$  weak coupling constant

$w(\cos \varphi_{eb,db})$  angular distribution of the W decay

$$\omega(x) = m_t^2 \left[ (1 - x^2) + \frac{m_W^2}{m_t^2} (1 + x)^2 \right] ; \quad x = \cos \varphi_{eb,db} \text{ in the } W \text{ frame}$$

# Angular Distribution of Top Decay Products

$$w(\cos\phi) = F_- \frac{3}{4}(1 - \cos\phi)^2 + F_0 \frac{3}{4}(1 - \cos^2\phi) + F_+ \frac{3}{4}(1 + \cos\phi)^2$$



similar case for the hadronic decay of the  $W$

In SM (with  $m_b=0$ ),

$$F_- = \frac{2\alpha}{1+2\alpha}$$

$$F_- = 0.3$$

We want to extract

$$F_0 = \frac{1}{1+2\alpha}$$

$$F_0 = 0.7$$

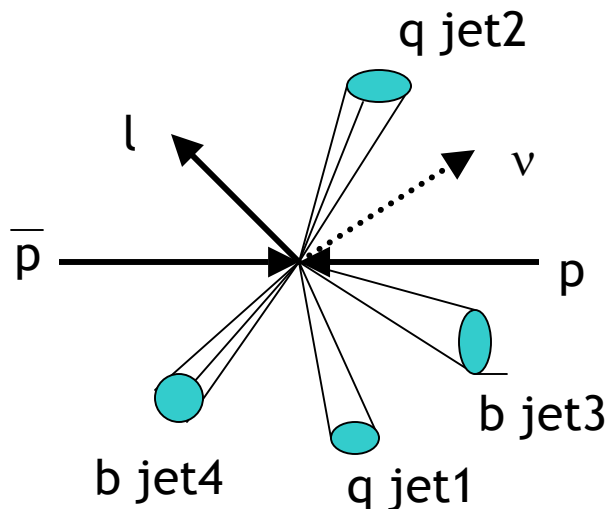
$$F_+ = 0$$

$$F_+ = 0$$

where  $\alpha = M_W^2/M_{\text{top}}^2$

with  $M_{\text{top}} = 175$  GeV and  $M_W = 80.4$  GeV

# Probability for Signal Events



- $2(in) + 18(final) = 20$  degrees of freedom
- $3(e) + 8(\Omega_1 \dots \Omega_4) + 3(P_{in} = P_{final}) + 1(E_{in} = E_{final}) = 15$  constraints
- $20 - 15 = 5$  integrals  $\Rightarrow$  we choose  $M_{top}$ ,  $m_W$  and jet energy of one of the jets because  $|M|^2$  is almost negligible, except near the four peaks of the Breit-Wigners within  $|M|^2$
- All the neutrino all possible solutions are considered
- Sum over 12 combinations of jets

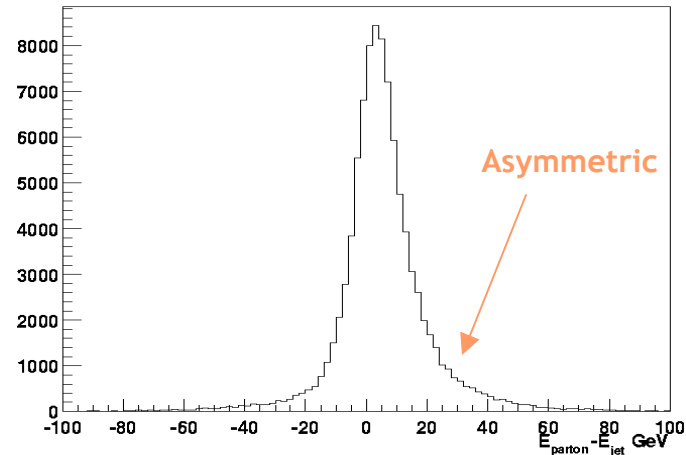
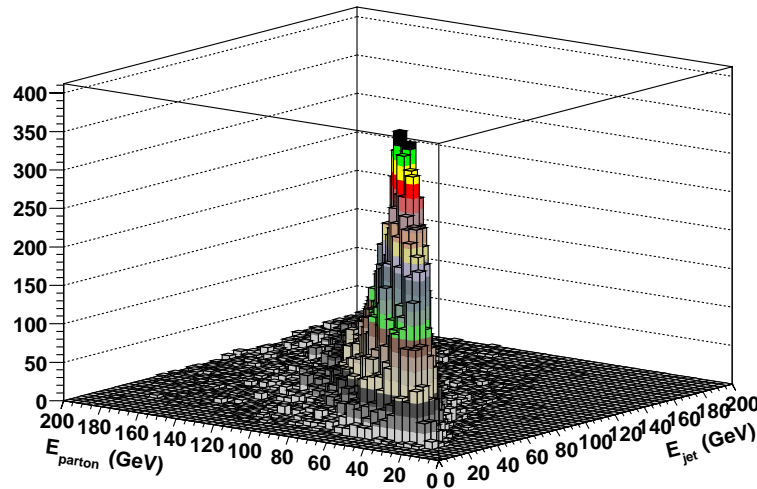
$$P_{t\bar{t}}(x, \alpha) = \frac{1}{12\sigma_{t\bar{t}}} \int d\rho_1 dm_1^2 dM_1^2 dm_2^2 dM_2^2 \sum_{comb, \nu} |M_{t\bar{t}}(\alpha)|^2 \frac{f(q_1)f(q_2)}{|q_1||q_2|} \phi_6 W_{jet}(x, y)$$

- $\rho_1$  momentum of one of the jets
- $m_1, m_2$  top mass in the event
- $M_1, M_2$  W mass in the event
- $f(q_1), f(q_2)$  parton distribution function (CTEQ4) for incident partons
- $q_1, q_2$  initial parton momentum
- $\phi_6$  six particle phase space
- $W_{jet}(x, y)$  probability of measuring x when y was produced in the collision

# Probability for Background Events

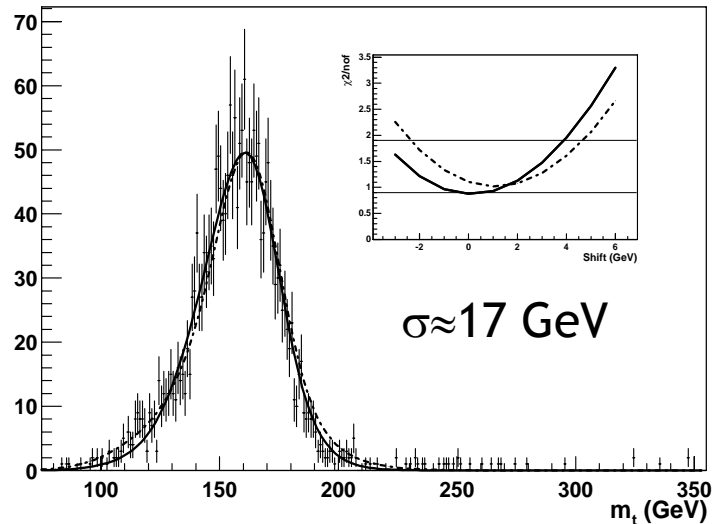
- ❖ The background probability is defined only in terms of the main background ( $W$ +jets, 85%) which proves to be an adequate representation for multijet background
- ❖ The background probability for each event is calculated using **VECBOS subroutines for  $W$ +jets**
- ❖ Same **transfer functions** for modeling the jet resolutions  $W(x,y)$  as for signal events
- ❖ **All permutations** are considered, together with the possible values of the  $z$  component of the momentum of the neutrino
- ❖ Integration done over the jet energies (very slow calculation)
- ❖ Monte Carlo method of integration. Integrate until ensure convergence.

# Transfer Functions $W_{jet}(x,y)$

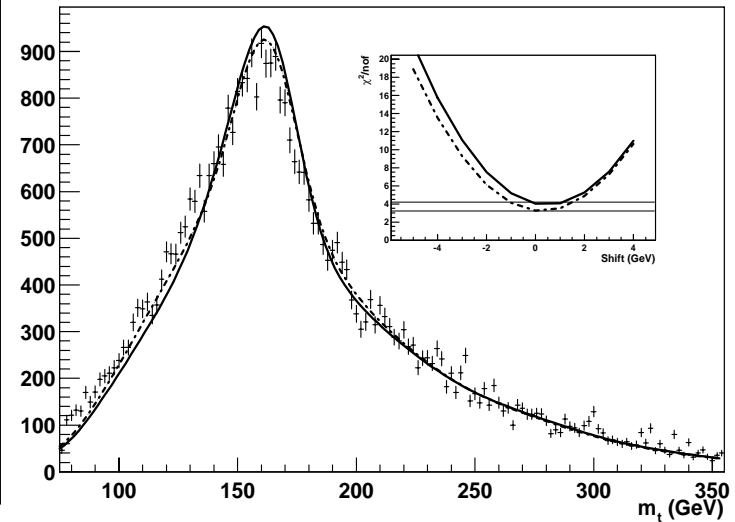


- Model the smearing in jet energies from effects of **radiation, hadronization, measurement resolution, and jet reconstruction algorithm**
  - Use **2 Gaussians**, one to account for the peak and the other to fit the asymmetric tails,
- $$W_{jet}(x,y) = \frac{1}{\sqrt{2\pi}(p_1 + p_2 p_5)} \left[ \exp \frac{-(\delta_E - p_1)^2}{2p_2^2} + p_3 \exp \frac{-(\delta_E - p_4)^2}{2p_5^2} \right] \quad \text{where} \quad p_i = a_i + b_i E_{parton}$$
- Parameters are obtained from maximizing a likelihood and using different samples of Monte Carlo events where jets were matched to partons
  - $b$  and light quark jets

## Best Case Scenario



## Worst Case Scenario



### Top Mass

**Histogram:** HERWIG Monte Carlo DØ Run I simulation and reconstruction with standard selection criteria

**Solid line:** Exact calculation using the transfer functions

- |   |   |
|---|---|
| <ul style="list-style-type: none"> <li>• Only events matched to partons (50%) are used in these histograms</li> <li>• Only correct permutation is considered</li> </ul> | <ul style="list-style-type: none"> <li>• Events with exactly 4 jets</li> <li>• No matching to partons was required</li> <li>• 12 permutations are considered</li> </ul> |
|---|---|

## Approximations in the probabilities definitions (things to do better with more statistics)

- **Only  $t\bar{t}b\bar{a}r$  from  $q\bar{q}b\bar{a}r$  production:** it does not include 10% of  $t\bar{t}b\bar{a}r$  events that are produced by gluon fusion
- **Only  $W$ +jets background:** that is ~85% only of the background
- **Leading-Order  $t\bar{t}b\bar{a}r$  matrix element:** no extra jets, constrains our sample to have only 4 jets

$$P_0(x; c_1, c_2, \alpha) = c_1 P_{t\bar{t}b\bar{a}r}(x; \alpha) + c_2 P_{W+jets}(x)$$

After these approximations, the likelihood function used is

$$-\ln L(\alpha) = -\sum_{i=1}^N \ln [c_1 P_{t\bar{t}b\bar{a}r}(x_i; \alpha) + c_2 P_{W+jets}(x_i)] + N \int A(x) [c_1 P_{t\bar{t}b\bar{a}r}(x; \alpha) + c_2 P_{W+jets}(x)] dx$$

The values of  $c_1$  and  $c_2$  are optimized, and the likelihood is normalized automatically at each value of  $\alpha$

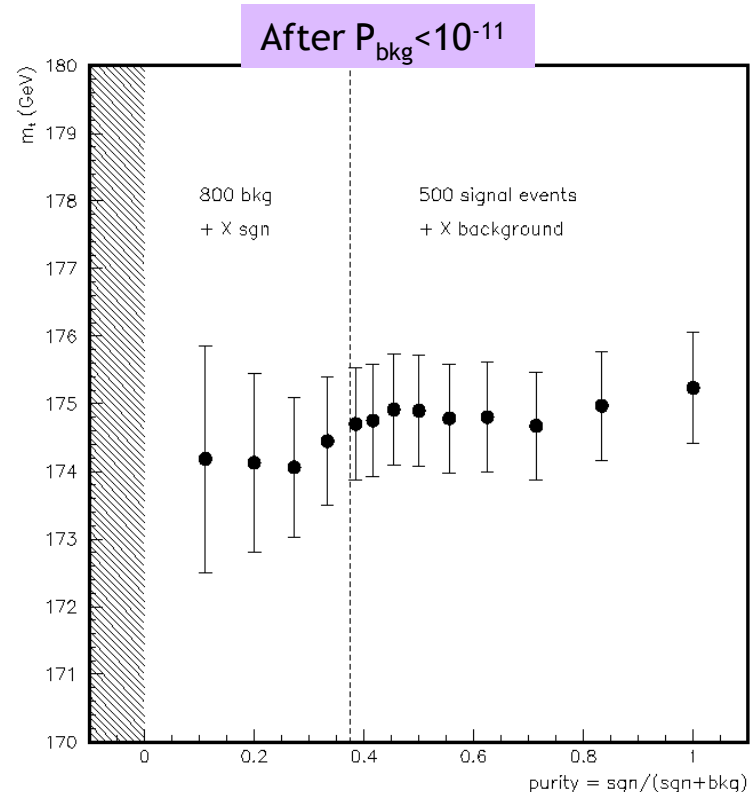
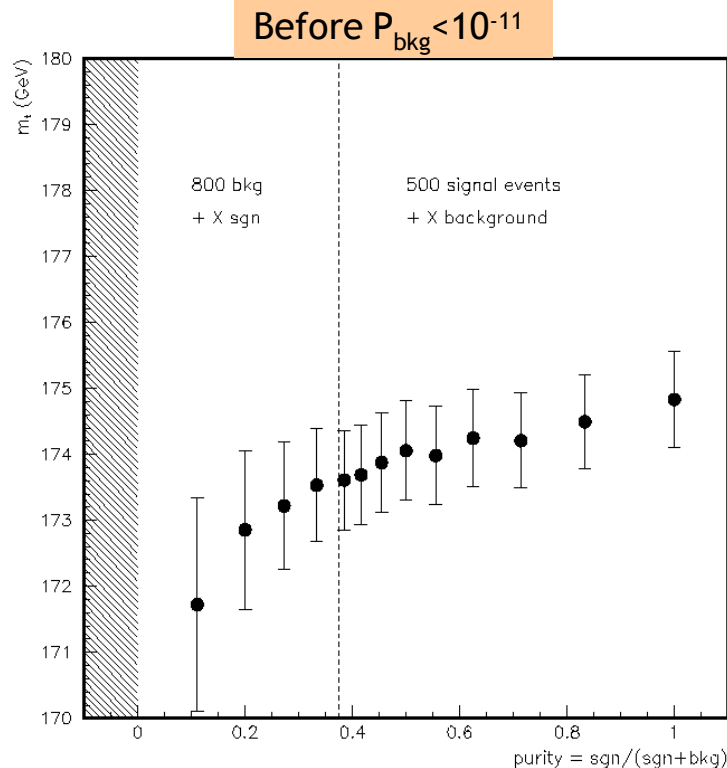
Depends on  $\alpha$

Constant

Calculated in two different ways  
using Monte Carlo method of  
integration

# Blind Analysis, purified sample

- This analysis was defined by MC studies, without looking at the data sample
- One of the checks indicated that there could be a shift introduced by background contamination



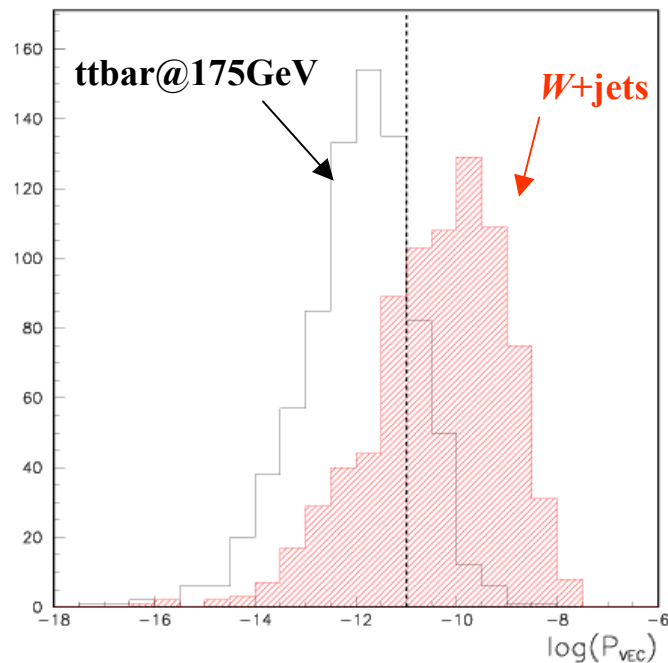


## Extra Selection in $P_{bkg}$

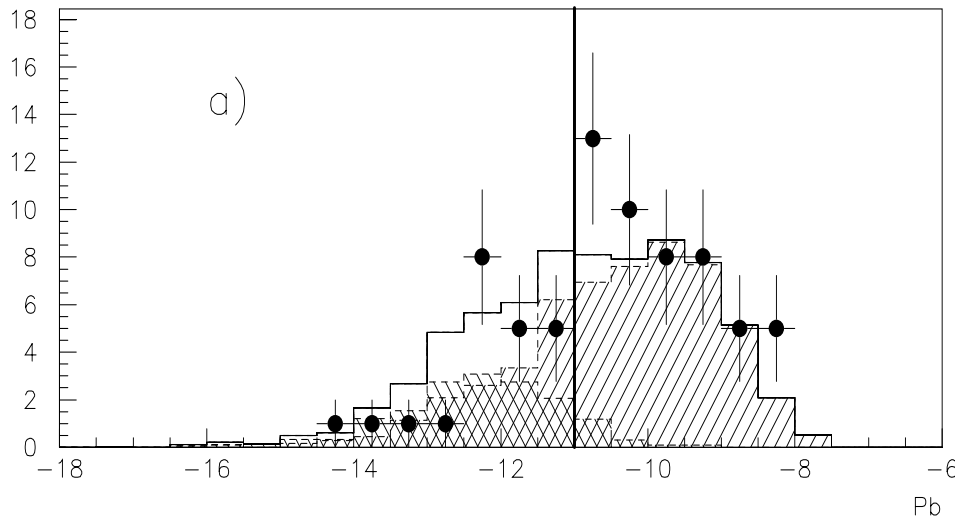
- In order to increase the purity of signal another selection is applied on  $P_{bkg}$ , with efficiencies:

$$\begin{aligned}\epsilon_{t\bar{t}} &= 0.70, \\ \epsilon_{W+jets} &= 0.30, \\ \epsilon_{multijets} &= 0.23\end{aligned}$$

- We select on  $P_{bkg} < 10^{-11}$ , according to a previous analysis done with this method to measure the top mass



# Signal / Background Discrimination

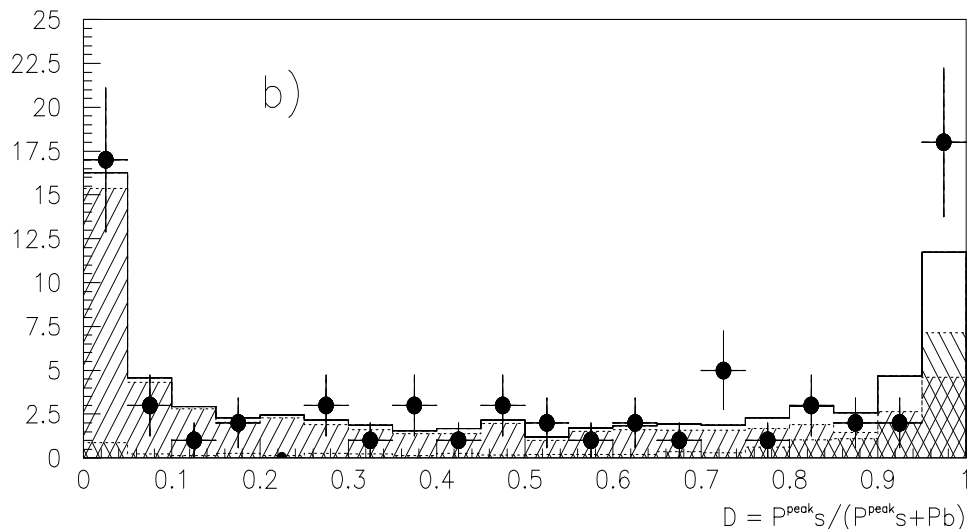


- Comparison of (16 Signal + 55 Background) MC and data sample

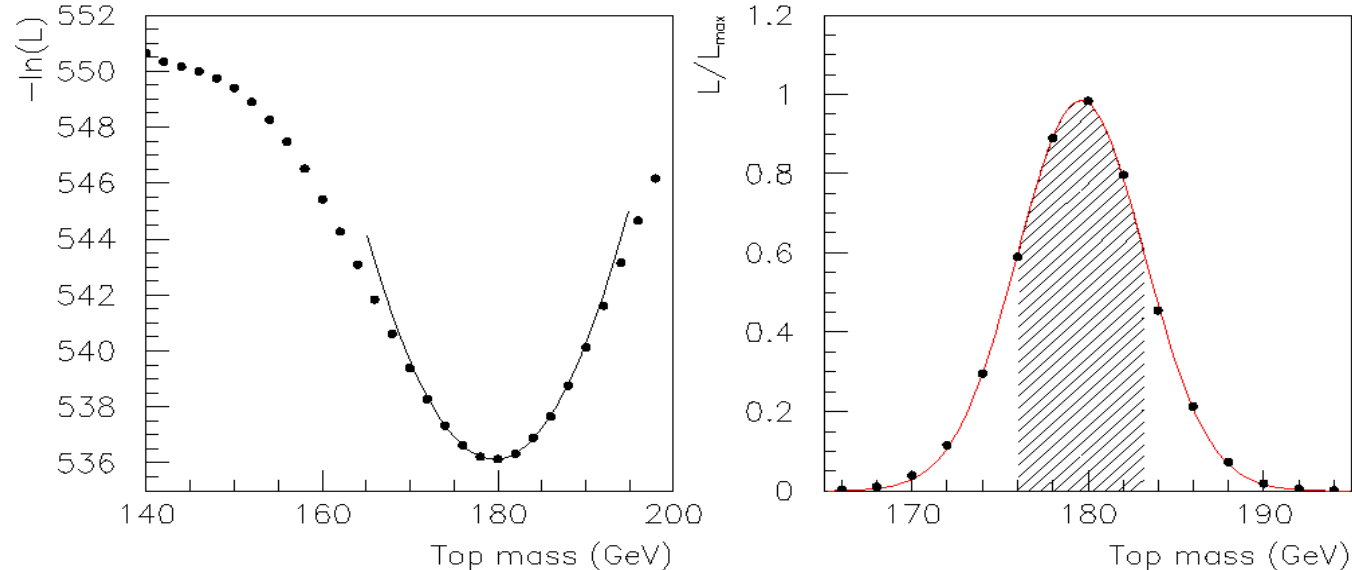
a) Background probability comparison between data (dots) and MC (histogram).

b) Signal probability comparison between data (dots) and MC (histogram) in the form of a discriminant

$$D = P_{\text{signal}} / (P_{\text{signal}} + P_{\text{background}})$$



# Preliminary Measurement of $M_{top}$ with $D\bar{D}$ Run I Data



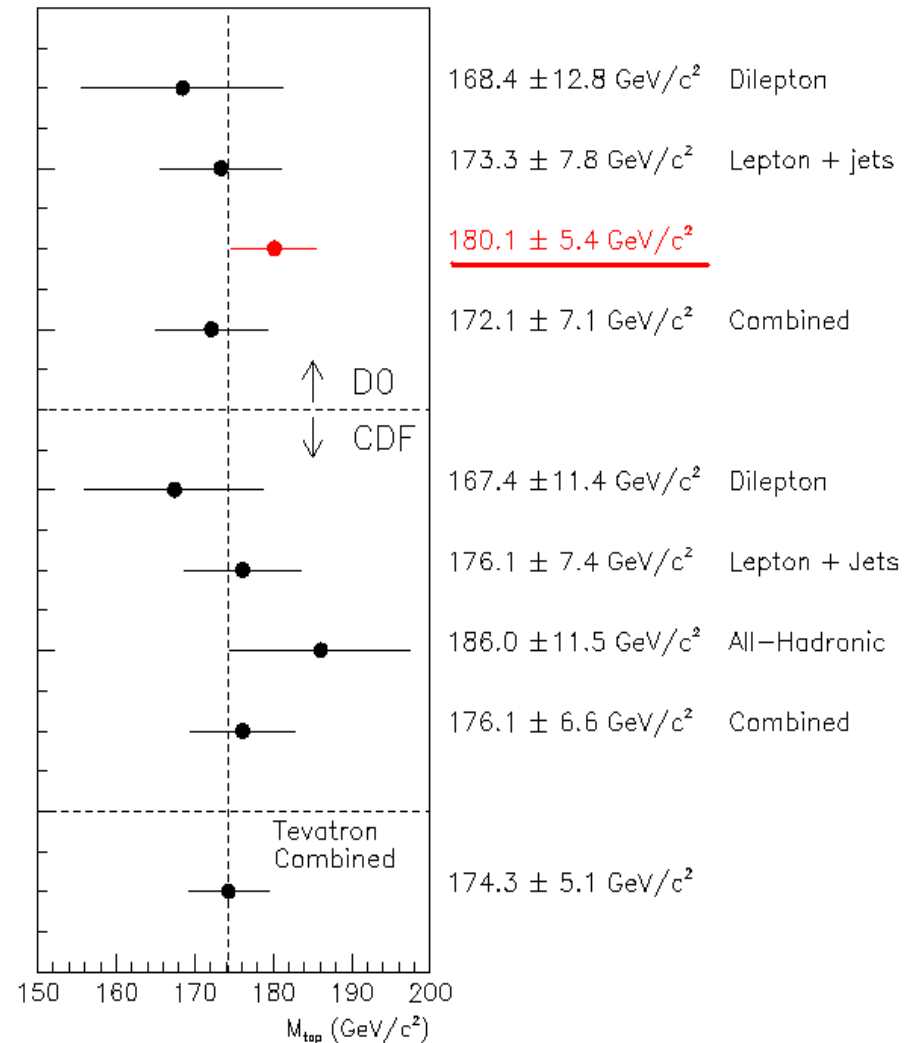
$$M_{top} \text{ (preliminary)} = 180.1 \pm 3.6_{\text{stat}} \pm 4.0_{\text{syst}} \text{ GeV}$$

- This new technique improves the statistical error on  $M_{top}$  from 5.6 GeV [PRD 58 52001, (1998)] to 3.6 GeV
- This is equivalent to a factor of 2.4 in the number of events

MC	Signal model	1.5 GeV
	Background model	1.0 GeV
	Noise and multiple interactions	1.3 GeV
DATA	Jet Energy Scale	3.3 GeV
	Parton Distribution Function	0.2 GeV
	Acceptance Correction	0.5 GeV

# New [preliminary] Result

- The relative error in this result is 3%, compare to 2.9% from the previous CDF and DØ combined average for all channels

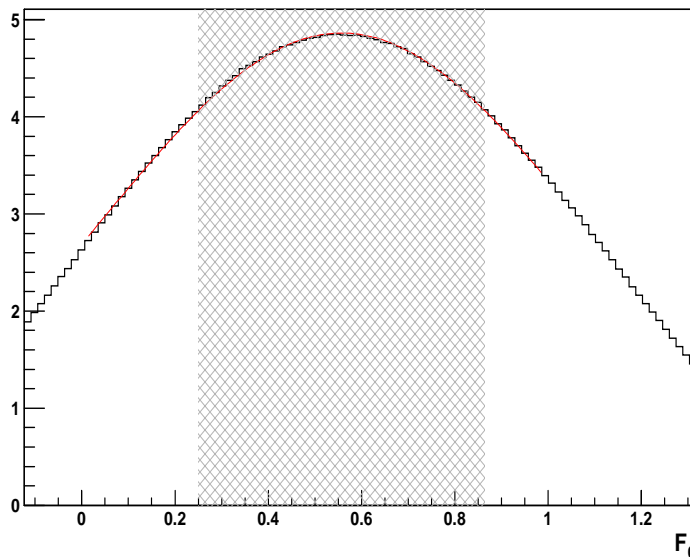


# Preliminary Measurement of $F_0$ with $D\bar{D}$ Run I Data

- Uncertainty on the top mass translates into a systematic error on the measurement of  $F_0$
- We integrate over  $M_{\text{top}}$  from 165 to 190 GeV (no prior)

$$L(F_0) = \int L(M_{\text{top}}, F_0) dM_t$$

- Integrated over  $\mu$  resolution
- 35  $e$ +jets candidates
- 36  $\mu$ +jets candidate



$$F_0 \pm \delta F_0(\text{Stat} + M_{\text{top}}) = 0.558 \pm 0.306$$

**From data**

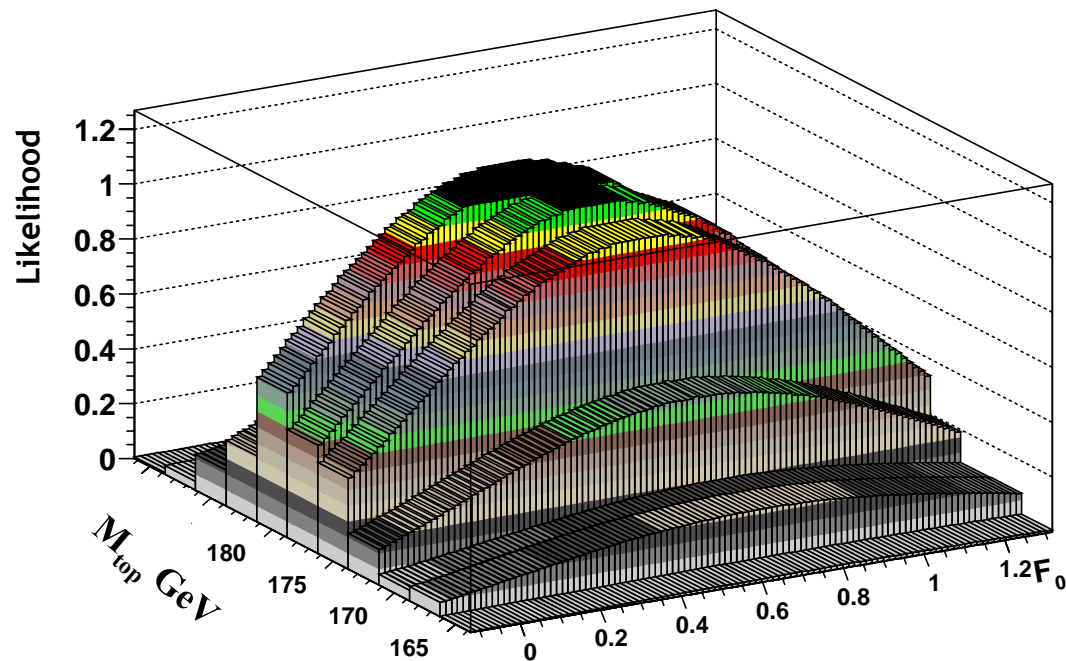
Statistics + $M_{\text{top}}$ uncertainty	0.306
Jet Energy Scale	0.014
Parton Distribution Function	0.007
Acceptance-Linearity Correction	0.021

**From Monte Carlo**

Background	0.010
Signal Model	0.020
Multiple Interactions	0.009
$t\bar{t}$ Spin Correlations	0.008

## Two-dimensional Probability - $M_{top}$ , $F_0$

- Assuming  $F_0 = 0.7$  (SM),  $M_{top}$  is measured to be  $180.1 \pm 3.6$  GeV (shift of 0.5 GeV applied)
- Assuming  $M_{top} = 175$  GeV,  $F_0$  is measured to be  $0.599 \pm 0.302$  (linearity response applied)



# Conclusions

- ❖ This method allows us to extract  $M_{\text{top}}$  and  $F_0$  using the **maximal information** in the event:
  - ✓ Correct permutation is always considered (along with the other eleven)
  - ✓ All features of individual events are included, thereby well measured events contribute more information than poorly measured events
- ❖ We made use of many approximations, LO ME and parameterized showering, we calculated the event probabilities, and measured:

$$M_{\text{top}}(\text{preliminary}) = 180.1 \pm 3.6 (\text{stat}) \pm 4.0 (\text{syst}) \text{ GeV}$$

$$F_0 (\text{preliminary}) = 0.56 \pm 0.31$$

- ❖ A complete calculation has to include:
  - the production of extra jets due to radiation, merging and/or splitting of jets
  - calculation of probabilities for every background process